## Shifting in Major League Baseball

## Introduction

"It's not hard to be romantic about baseball," is an often-quoted line from 2011 movie Moneyball, and it is a statement that is simply true. There is something in the air at a ball field, from the most highly funded stadium to the overgrown outfield of a small town's field, something that makes everything feel a little simpler, a little more like childhood and happiness. In the rush of a game, there is nothing that matters but the ball and the base, and perhaps the scoreboard. But baseball is also much more than that, it is a complex game with rules that require both instinct and intellect, and an ability to adapt to any situation that arises. With this idea comes the ever-changing strategies of the game, from the beginnings of batting statistics in 1917 to the development of statistical recruiting in 2003 (Lee, 2018). One of the most recent developments in fielding, however, is the concept of "shifting," or the movement of the majority infielders to one side of the field based on where each individual batter is most probable to hit.

Shifting has only become popular in the last decade, first being used to remarkable success by the Tampa Bay Rays in their 2010 season. Much like the statistical hirings developed in 2003 by the Oakland A's, shifting was a strategy built because of budget. The Tampa Bay Rays in 2010 needed a way to win games on a budget much smaller than many of their competitors, and from this need came the idea of moving fielders to only the spots where a batter was likely to hit - why use a valuable player in a place where they are improbable to be useful when there is so much more to gain in having them placed somewhere else (Heyen, 2020). And it worked - according to Bill Heyen of Sporting News, between 2009 and 2011, opponents of the Rays had hits $1.2 \%$ less than the league average. Since the Rays first success using this strategy, the form has only grown more popular, with every team in Major League Baseball (MLB) using it in the 2021 season and has become a controversial topic amongst baseball fans due to this.

The initial goal of this paper was to investigate certain aspects of the claims made against shifting, and demonstrating the statistical realities of the effect of shifting on teams based on win/loss
proportion and funding, as well as it's effect on individual batters. However, when progressing in the paper, I have found other aspects which lead me to investigate the best model of MLB ranking based on win/loss proportion vs the shifting proportion of teams in 2019. To do this, I plan to run various kinds of regressions on the total data of the 30 MLB teams, looking specifically at their ranking and at the proportion of plate appearances they shifted on. To collect the data for this modeling exploration, I will use the information collected by Baseball Savant, which is a database specifically made by the MLB and which stores vast amounts of data about the MLB teams. Too, I will be sourcing my data from the 2019 season, as at the time of writing it is the most recently completed full season, and therefore the most truly accurate and relevant data available. In total, my goal is to better understand the relationship between the proportion of shifting and the win/loss rates of the various major league teams.

## Data Collection and Initial Findings

As previously stated, to get data for this project, I used sites such as Baseball Savant and Baseball Reference to collect information on teams ranking and shift rate. Information on the payroll - the amount of money the team paid to its players over the course of the season - of specific teams was collected from SpoTrac and used to operationalize the funding of teams. All this data has been compiled in a variety of tables, which are displayed below.

Table 1 shows the top ten and bottom ten ranked teams of the MLB in 2019 and the percentage of plays they shifted on out of the plate appearances in the season.

| TEAM NAME | RANKING | SHIFT PER <br> PLAY (\%) |
| :--- | ---: | ---: |
| ASTROS | 1 | 49.5 |
| DODGERS | 2 | 50.6 |
| YANKEES | 3 | 36 |
| TWINS | 4 | 35.5 |
| ATHLETICS | 5 | 19.2 |
| BRAVES | 6 | 14.9 |
| RAYS | 7 | 37.2 |
| INDIANS | 8 | 14 |
| NATIONALS | 9 | 14.3 |
| CARDINALS | 10 | 15.8 |
| ANGELS | 21 | 16.8 |
| ROCKIES | 22 | 18.7 |
| PADRES | 23 | 16.7 |
| PIRATES | 24 | 30.2 |
| MARINERS | 25 | 19.1 |
| BLUE JAYS | 26 | 28.5 |
| ROYALS | 27 | 17.9 |
| MARLINS | 28 | 36.4 |
| ORIOLES | 29 | 42.8 |
| TIGERS | 30 | 29.3 |

Table 1

We can see from this table that the top two teams in 2019, the Astros and the Dodgers, have the highest shift per play (SpP) percentage of these twenty 2019 teams at $49.5 \%$ and $50.6 \%$. Meanwhile, in the
bottom half of the ranking, teams like the Orioles managed to place in the top 10 highest shift rates while maintaining a spot in the bottom 10 in terms of win/loss rate. The overall mixed use of shifting leads to no apparent correlations between the shift and ranking just by looking at the data. To better display this data however, I went through the process of placing the data into graphs.

Due to the generally decreasing SpP rates in the top ten teams, I suspected that the graph would follow a linear trend. To be able to prove linearity, we must calculate $r$ using the formula:

$$
r=\frac{1}{n-1} \sum\left(\frac{x_{i}-\bar{x}}{s_{x}}\right)\left(\frac{y_{i}-\bar{y}}{S_{y}}\right)
$$

with

$$
\bar{x}=\frac{1+2+3+4+5+6+7+8+9+10}{10}=\frac{11}{2}
$$

$$
s_{x}=\sqrt{\frac{\begin{array}{c}
\left(1-\frac{31}{2}\right)^{2}+\left(2-\frac{31}{2}\right)^{2}+\left(3-\frac{31}{2}\right)^{2}+\left(4-\frac{31}{2}\right)^{2}+\left(5-\frac{31}{2}\right)^{2}+\left(6-\frac{31}{2}\right)^{2}+\left(7-\frac{31}{2}\right)^{2}+\left(8-\frac{31}{2}\right)^{2}+\left(9-\frac{31}{2}\right)^{2}+ \\
\left(10-\frac{31}{2}\right)^{2}
\end{array} 30}{30}}=6.01
$$

$$
\bar{y}=\frac{49.5+50.6+36+35.5+19.2+14.9+37.2+14+14.3+15.8}{10}=28.7
$$

$$
s_{y}=
$$

$\sqrt{\frac{(49.5-25.6)^{2}+(50.6-25.6)^{2}+(36-25.6)^{2}+(35.5-25.6)^{2}+(19.2-25.6)^{2}+(14.9-25.6)^{2}+(37.2-25.6)^{2}+(14-25.6)^{2}+(14.3-25.6)^{2}+(15.8-25.6)^{2}}{30}}$

Resulting in a final equation of:

$$
\begin{gathered}
r=\frac{1}{10-1}\left(\left(\left(\frac{1-5.5}{6.01}\right)\left(\frac{49.5-28.7}{8.26}\right)\right)+\left(\left(\frac{2-5.5}{6.01}\right)\left(\frac{50.6-28.7}{8.26}\right)\right)+\left(\left(\frac{3-5.5}{6.01}\right)\left(\frac{36-28.7}{8.26}\right)\right)+\right. \\
\left(\left(\frac{4-5.5}{6.01}\right)\left(\frac{35.5-28.7}{8.26}\right)\right)+\left(\left(\frac{5-5.5}{6.01}\right)\left(\frac{19.2-28.7}{8.26}\right)\right)+\left(\left(\frac{6-5.5}{6.01}\right)\left(\frac{14.9-28.7}{8.26}\right)\right)+\left(\left(\frac{7-5.5}{6.01}\right)\left(\frac{37.2-28.7}{8.26}\right)\right)+ \\
\left.\left(\left(\frac{8-5.5}{6.01}\right)\left(\frac{14-28.7}{8.26}\right)\right)+\left(\left(\frac{9-5.5}{6.01}\right)\left(\frac{14.3-28.7}{8.26}\right)\right)+\left(\left(\frac{10-5.5}{6.01}\right)\left(\frac{15.8-28.7}{8.26}\right)\right)\right)=-0.746
\end{gathered}
$$

With this r value being above |0.7| there is a strong negative correlation between rank and shifting rate in the top ten MLB teams. Because of this, I put the data into a scatterplot in Graph 1, which further revealed a negative correlation trend, and when looking at the graph we can see what looks to be a linear trend. With this hypothesis of linearity, I moved onto a residuals plot, displayed in Graph 2, where we can see an approximately random scatter, which further implicates the linearity of the data correlation. Because of all these factors, running a linear regression is viable, and results in the equation of $y=$ $50.92-4.04 x$. This equation results in an $r^{2}$ value of 0.68 , which means that the least-squared regression line (LSRL) explains $68 \%$ of variation in $y$ or SpP .


Graph 2


Graph 1

A similar process was gone through with the bottom ten teams in the MLB, with the r value calculations being largely similar, though the workings aren't shown in full here. With this, we see an $r$ value of 0.7 , equating to a strong positive correlation. I again then put the data into a scatterplot in Graph 3 , where there is what appears to be a positive linear trend. When this is transferred to a residual plot in Graph 4, the trend maintains its relevance, as the plot is randomly scattered, and therefore a linear regression is possible.

When the regression is run, the result is $y=-28.7+2.13 x$ and have a $r^{2}$ value of 0.49 and is therefore only accounting for $49 \%$ of variation.

These two sets of data interestingly are opposite to one in terms of correlation direction, despite coming from the same overall population, though on different ends. I also noticed that the $10^{\text {th }}$ and $21^{\text {st }}$ ranked teams have SpP rates which are only separated by $1 \%$, and if graphed on the same graph, would be the same distance to the x -axis from an axis of symmetry for a quadratic function. Noticing this phenomenon and having access to the intermediate ten data points which would make this a complete data


Graph 4


Graph 3 set, I chose to expand my initial plan to create a model to understand the total relationship between shifting and the win/loss rate of teams in the 2019 season.


To look at what potential model it could be, I began to run regressions of various kinds, looking for the model with the highest $r$ value. These various regressions, their modeled formula, $r$ values, and $r^{2}$ values are all displayed in

| REGRESSION | EQUATION | $\boldsymbol{r}$ | $\boldsymbol{r}^{2}$ |
| :--- | :---: | :---: | :---: |
| NAME |  |  |  |
| LINEAR | $y=0.172+0.169 x$ | 0.153 | 0.023 |
| QUADRATIC | $y=6.64 x^{2}-6.34 x+1.7$ | 0.652 | 0.426 |
| CUBIC | $y=35.8 x^{3}-44.9 x^{2}+17.7 x-1.91$ | 0.738 | 0.545 |
| QUARTIC | $y=95.2 x^{4}-148 x^{3}+84.6 x^{2}-22 x+2.52$ | 0.744 | 0.553 |
| POWER | $y=0.238 x^{0.0171}$ | 0.00598 | 0.0000358 |
| EXPONENTIAL | $y=0.205(1.33)^{x}$ | 0.0687 | 0.00472 |
| LOGARITHMIC | $y=0.288+0.0441(\log x)$ | 0.0848 | 0.0072 |

Table 3

Table 3. As one can see demonstrated in the table, the $r$ value is highest for the power model graphs, with the highest of those being the quartic model at an $r$ value of 0.744 . This means that using the quartic model, there would be an estimated $74.4 \%$ correlation, and because of the $r^{2}$ value of 0.553 , the model accounts for $55.3 \%$ of variation.

Because the quartic model only has an $r$ value of 0.738 , which, while being a strong correlation, is a fairly low correlation in comparison to the possible $r$ values if we continue to increase the polynomial order. To attempt to find the regression models, as the graphing calculator used with the initial regressions does not go past a quartic power model, I first attempted to use systems of equations and matrices and then calculate the $r$ and $r^{2}$.

To test what powers might work best, I can work with systems of equations and matrices in order to create models and then calculate the $r$ and $r^{2}$ value of the model. The first system of equations for the model $y=a x^{5}+b x^{4}+c x^{3}+d x^{2}+e x+f$ is displayed below.

$$
\begin{gathered}
0.495=a(.66)^{5}+b(.66)^{4}+c(.66)^{3}+d(.66)^{2}+e(.66)+f \\
0.506=a(.654)^{5}+b(.654)^{4}+c(.654)^{3}+d(.654)^{2}+e(.654)+f \\
0.325=a(.525)^{5}+b(.525)^{4}+c(.525)^{3}+d(.525)^{2}+e(.525)+f \\
0.127=a(.519)^{5}+b(.519)^{4}+c(.519)^{3}+d(.525)^{2}+e(.525)+f \\
0.428=a(.333)^{5}+b(.333)^{4}+c(.333)^{3}+d(.333)^{2}+e(.333)+f \\
0.364=a(.352)^{5}+b(.352)^{4}+c(.352)^{3}+d(.352)^{2}+e(.352)+f
\end{gathered}
$$

I then reduced the equations, which are also displayed below.

$$
\begin{gathered}
0.495=0.125 a+0.19 b+0.287 c+0.436 d+0.66 e+f \\
0.506=0.12 a+0.183 b+0.28 c+0.428 d+0.654 e+f \\
0.325=0.0399 a+0.76 b+0.145 c+0.276 d+0.525 e+f \\
0.127=0.0377 a+0.0726 b+0.14 c+0.269 d+0.519 e+f \\
0.428=0.0041 a+0.0122 b+0.0369 c+0.111 d+0.333 e+f \\
0.364=0.0054 a+0.0154 b+0.0436 c+0.124 d+0.352 e+f
\end{gathered}
$$

From here, the new coefficients must be inserted into a matrix, where the coefficients of each system are placed in order, then multiplied by a second matrix of the variables, which are equal the solutions to the systems. This is all displayed in the matrix below.

| 0.125 | 0.19 | 0.287 | 0.436 | 0.66 | 1 | $a$ | 0.495 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.12 | 0.183 | 0.28 | 0.428 | 0.654 | 1 | $b$ | 0.506 |
| 0.0399 | 0.76 | 0.145 | 0.27 | 0.525 | 1 |  |  |
| 0.0377 | 0.0726 | 0.14 | 0.269 | 0.519 | 1 | ${ }^{c}=$ | 0.325 |
| 0.0041 | 0.0122 | 0.0369 | 0.111 | 0.333 | 1 | $e$ | 0.127 |
| 0.0054 | 0.0154 | 0.0436 | 0.124 | 0.352 | 1 | $f$ | 0.364 |

This is all then calculated using the matrix function in a graphing calculator, coming to the following results for each variables posited solution; $a=-648, b=626, c=1040, d=-1501, e=595, f=$ -74.7. Thus, the regression line for a power model with the highest power of 5 would be:

$$
y=-58.6 x^{5}+30.3 x^{4}+91.2 x^{3}-89.6 x^{2}+24.7 x-1.33
$$

To finish out this problem, I must calculate the $r$ and $r^{2}$ values of the equation. To calculate $r$ the following equation must be employed:

$$
r=\frac{1}{n-1} \sum\left(\frac{x_{i}-\bar{x}}{s_{x}}\right)\left(\frac{y_{i}-\bar{y}}{s_{y}}\right)
$$

with

$$
\bar{x}=\frac{1+2+3+4+5+6+7+8+9+10+11+12+13+14+15+16+17+18+19+20+21+22+23+24+25+26+27+28+29+30}{30}=15.5
$$

$$
s_{x}=
$$

$$
\sqrt{\left(1-\frac{31}{2}\right)^{2}+\left(2-\frac{31}{2}\right)^{2}+\left(3-\frac{31}{2}\right)^{2}+\left(4-\frac{31}{2}\right)^{2}+\left(5-\frac{31}{2}\right)^{2}+\left(6-\frac{31}{2}\right)^{2}+\left(7-\frac{31}{2}\right)^{2}+\left(8-\frac{31}{2}\right)^{2}+\left(9-\frac{31}{2}\right)^{2}+\left(10-\frac{31}{2}\right)^{2}+\left(11-\frac{31}{2}\right)^{2}+\left(12-\frac{31}{2}\right)^{2}+\left(13-\frac{31}{2}\right)^{2}+}
$$

$$
\left(14-\frac{31}{2}\right)^{2}+\left(15-\frac{31}{2}\right)^{2}+\left(16-\frac{31}{2}\right)^{2}+\left(17-\frac{31}{2}\right)^{2}+\left(18-\frac{31}{2}\right)^{2}+\left(19-\frac{31}{2}\right)^{2}+\left(20-\frac{31}{2}\right)^{2}+\left(21-\frac{31}{2}\right)^{2}+\left(22-\frac{31}{2}\right)^{2}+\left(23-\frac{31}{2}\right)^{2}+\left(24-\frac{31}{2}\right)^{2}+\left(25-\frac{31}{2}\right)^{2}+
$$

$$
\sqrt{\frac{\left(26-\frac{31}{2}\right)^{2}+\left(27-\frac{31}{2}\right)^{2}+\left(28-\frac{31}{2}\right)^{2}+\left(29-\frac{31}{2}\right)^{2}+\left(30-\frac{31}{2}\right)^{2}}{30}}
$$

$$
\bar{y}=\frac{\begin{array}{l}
49.5+50.6+36+35.5+19.2+14.9+37.2+14+14.3+15.8+34.1+14.1+32.5+18.4+12.7+ \\
17.1+21.4+25.4+27+22.3+16.8+18.7+16.7+30.2+19.1+28.5+17.9+36.4+42.8+29.3
\end{array}}{30}=25.6
$$

$$
s_{y}=
$$

$\sqrt{$| $(49.5-25.6)^{2}+(50.6-25.6)^{2}+(36-25.6)^{2}+(35.5-25.6)^{2}+(19.2-25.6)^{2}+(14.9-25.6)^{2}+(37.2-25.6)^{2}+(14-25.6)^{2}+(14.3-25.6)^{2}+$ |
| :---: |
| $(15.8-25.6)^{2}+(34.1-25.6)^{2}+(14.1-25.6)^{2}+(32.5-25.6)^{2}+(18.4-25.6)^{2}+(12.7-25.6)^{2}+(17.1-25.6)^{2}+(21.4-25.6)^{2}+(25.4-25.6)^{2}+$ |
| $(27-25.6)^{2}+(22.3-25.6)^{2}+(16.8-25.6)^{2}+(18.7-25.6)^{2}+(16.7-25.6)^{2}+(30.2-25.6)^{2}+(19.1-25.6)^{2}+(28.5-25.6)^{2}+(17.9-25.6)^{2}+$ |
| $(36.4-25.6)^{2}+(42.8-25.6)^{2}+(29.3-25.6)^{2}$ |$} 30$

Which gives us a final equation of:

$$
\begin{aligned}
& r=\frac{1}{30-1}\left(\left(\left(\frac{1-15.5}{8.66}\right)\left(\frac{49.5-25.6}{10.6}\right)\right)+\left(\left(\frac{2-15.5}{8.66}\right)\left(\frac{50.6-25.6}{10.6}\right)\right)+\left(\left(\frac{3-15.5}{8.66}\right)\left(\frac{36-25.6}{10.6}\right)\right)+\right. \\
& \left(\left(\frac{4-15.5}{8.66}\right)\left(\frac{35.5-25.6}{10.6}\right)\right)+\left(\left(\frac{5-15.5}{8.66}\right)\left(\frac{19.2-25.6}{10.6}\right)\right)+\left(\left(\frac{6-15.5}{8.66}\right)\left(\frac{14.9-25.6}{10.6}\right)\right)+\left(\left(\frac{7-15.5}{8.66}\right)\left(\frac{37.2-25.6}{10.6}\right)\right)+ \\
& \left(\left(\frac{8-15.5}{8.66}\right)\left(\frac{14-25.6}{10.6}\right)\right)+\left(\left(\frac{9-15.5}{8.66}\right)\left(\frac{14.3-25.6}{10.6}\right)\right)+\left(\left(\frac{10-15.5}{8.66}\right)\left(\frac{15.8-25.6}{10.6}\right)\right)+\left(\left(\frac{11-15.5}{8.66}\right)\left(\frac{34.1-25.6}{10.6}\right)\right)+ \\
& \left(\left(\frac{12-15.5}{8.66}\right)\left(\frac{14.1-15.5}{10.6}\right)\right)+\left(\left(\frac{13-15.5}{8.66}\right)\left(\frac{32.5-25.6}{10.6}\right)\right)+\left(\left(\frac{14-15.5}{8.66}\right)\left(\frac{18.4-25.6}{10.6}\right)\right)+\left(\left(\frac{15-15.5}{8.66}\right)\left(\frac{12.7-25.6}{10.6}\right)\right)+ \\
& \left(\left(\frac{16-15.5}{8.66}\right)\left(\frac{17.1-25.6}{10.6}\right)\right)+\left(\left(\frac{17-15.5}{8.66}\right)\left(\frac{21.4-25.6}{10.6}\right)\right)+\left(\left(\frac{18-15.5}{8.66}\right)\left(\frac{25.4-25.6}{10.6}\right)\right)+\left(\left(\frac{19-15.5}{8.66}\right)\left(\frac{27-25.6}{10.6}\right)\right)+ \\
& \left(\left(\frac{20-15.5}{8.66}\right)\left(\frac{22.3-25.6}{10.6}\right)\right)+\left(\left(\frac{21-15.5}{8.66}\right)\left(\frac{16.8-25.6}{10.6}\right)\right)+\left(\left(\frac{22-15.5}{8.66}\right)\left(\frac{18.7-25.6}{10.6}\right)\right)+\left(\left(\frac{23-15.5}{8.66}\right)\left(\frac{16.7-25.6}{10.6}\right)\right)+ \\
& \left(\left(\frac{24-15.5}{8.66}\right)\left(\frac{30.2-25.6}{10.6}\right)\right)+\left(\left(\frac{25-15.5}{8.66}\right)\left(\frac{19.1-25.6}{10.6}\right)\right)+\left(\left(\frac{26-15.5}{8.66}\right)\left(\frac{28.5-25.6}{10.6}\right)\right)+\left(\left(\frac{27-15.5}{8.66}\right)\left(\frac{17.9-25.6}{10.6}\right)\right)+ \\
& \left.\left(\left(\frac{28-15.5}{8.66}\right)\left(\frac{36.6-25.6}{10.6}\right)\right)+\left(\left(\frac{29-15.5}{8.66}\right)\left(\frac{42.8-25.6}{10.6}\right)\right)+\left(\left(\frac{30-15.5}{8.66}\right)\left(\frac{29.3-25.6}{10.6}\right)\right)\right)
\end{aligned}
$$

$$
r=-0.193
$$

As you can see, the $r$ value for the model generated using this method is incredibly low, and in no frame of mind would be seen as a valid way to model our data. This at first, confused me as I had checked over my work countless times. However, upon closer observation, this model and methodologies flaws become clear. To create this model, and any model like it, you must create six-variable systems of equations, which requires you to input six points of data to form said equation. The issue lies here, when
dealing with a sample of 30 - much larger than the available six points of data. Because of this, it is impossible to get a true accurate representation of the full sample being modeled after; my model used data points from both the highest, middling, and lowest ranking teams, which should theoretically offer the widest range of data, and still it resulted in an $r$ value of only $|0.193|$. Clearly, this systems of equations and matrices method is not viable for a data set as large as this.

| Due to this, I chose to instead use an online | POWER | EQUATION | $r$ | $r^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| calculator, which both uses the entirety of the data | 5 | $\begin{gathered} y=-0.0000317 x^{5}+0.003180 x^{4}-0.117 x^{3}+2 x^{2}-16 x \\ +68.7 \end{gathered}$ | 0.746 | 0.558 |
| set, and removes chances of deviation through | 6 | $\begin{gathered} y=-0.00000606 x^{6}+0.000532 x^{5}-0.0168 x^{4}+0.221 x^{3} \\ -0.734 x^{2}-6.62 x-59.5 \end{gathered}$ | 0.756 | 0.572 |
| rounding and other factors which are prevalent with | 7 | $\begin{array}{r} y=-0.000000146 x^{7}+0.00000973 x^{6}-0.000191 x^{4} \\ +0.0465 x^{3}+0.305 x^{2}-9.37 x-61.7 \end{array}$ | 0.757 | 0.573 |
| hand-done math. The results of these regressions - | 8 | $\begin{array}{r} y=-0.000000206 x^{8}+0.0000254 x^{7}-0.00129 x^{6}+0.539 x^{5} \\ -0.539 x^{4}+4.72 x^{3}-21.4 x^{2}+36.9 x-30.2 \end{array}$ | 0.786 | 0.618 |
| are displayed in Table 4 below. As we look at the | 9 | $\begin{aligned} y= & -0.0000000043 x^{9}+0.000000393 x^{8}-0.00000975 x^{7} \\ & -0.000164 x^{6}+0.0134 x^{5}-0.291 x^{4}+3.03 x^{3} \\ & -15.02 x^{2}+25.6 x+36.9 \end{aligned}$ | 0.787 | 0.619 |
| table, we can see that up to $x^{10}$ the $r$ value is steadily increasing, though it is beginning to level | 10 | $\begin{aligned} & y=-0.0000000015 x^{10}+0.000000230 x^{9}-0.0000152 x^{8} \\ &+0.000570 x^{7}-0.0134 x^{6}+0.205 x^{5}-2.04 x^{4} \\ &+12.8 x^{3}-45.7 x^{2}+72.6 x+11.7 \end{aligned}$ | 0.79 | 0.625 |
| we approach $x^{10}$ with only a 0.001 difference between the $r$ values of $x^{8}$ and $x^{9}$, and a 0.003 <br> difference between $x^{9}$ and $x^{10}$. However, after the | 11 | $\begin{aligned} & y=-0.0000000002 x^{11}+0.00000000307 x^{10}-0.00000216 x^{9} \\ &+0.0000858 x^{8}-0.00212 x^{7}+0.0335 x^{6} \\ &-0.334 x^{5}+1.99 x^{4}-6.04 x^{3}+5.05 x^{2}+4.09 x \\ &+45.2 \end{aligned}$ | 0.769 | 0.591 |

## Table 4

0.021 of a difference between the $r$ value of $x^{10}$ and $x^{11}$.

Through this, we can conclude that the best fitting model for the overall relationship between the ranking of win/loss and the SpP of plate appearances shifted on for all 30 MLB teams in the 2019 season is the $10^{\text {th }}$ power parabolic model, specifically:

$$
\begin{gathered}
y=-0.0000000015 x^{10}+0.000000230 x^{9}-0.0000152 x^{8}+0.000570 x^{7}-0.0134 x^{6}+0.205 x^{5} \\
-2.04 x^{4}+12.8 x^{3}-45.7 x^{2}+72.6 x+11.7
\end{gathered}
$$

To look more closely at this, I have graphed the model over the scatterplot in Graph 6 and removed the points on Graph 7. Overall, the model appears to fit the data quite well, with Graph 6 demonstrating that it largely follows the trends of the data, only seeming to have a few outliers which are more removed from the trendline in the top 15 teams. This model also shows, for the most part, that there is a power relationship between the two variables with an absolute maximum at the highest ranked teams and a clear relative maximum at the lowest ranked teams. We can also see that in the higher rankings, there is a sharp decline in shifting as the rankings go down, however at approximately $x=6$, the SpP rate begins to


Graph 6

Shift per Play \% vs. Ranking on Win/Loss Rate


Graph 7
level off until $x=26$, middling around $20 \%$
SpP for those teams ranked $6^{\text {th }}$ through $26^{\text {th }}$. We do see a mild relative maximum around $x=22$, immediately followed by the final rise to the second, more distinct, relative maximum at the lowest ranked teams. The graph also shows that while both the highest and lowest ranked teams tend to have SpP rates above the middling teams, the highest ranked teams are expected to shift a little over $10 \%$ more often than the lowest ranking teams. It also shows that it is likely only the top and bottom 5 teams who have SpP rates higher than middling teams, which goes against my initial hypothesis which posed that it would be the top and bottom 10 teams.

## Findings and Reflections

After analysis of the models created for the relationship between the ranking of MLB teams based off of win/loss rate and the SpP percentage, I have reached several conclusions about the nature of the shift's use in the MLB in the 2019 season and the most effective ways to model this phenomenon. First, I have learned much about the approaches used to create models, specifically methods involving systems of equations and matrices, which, while an interesting aspect of math and perhaps a good tool for small-sample-models when you lack a calculator, they failed to accurately portray data which is significantly larger than the variable slots. However, when transferring to a far more accurate calculation technique using a digital calculator, I found that the power model of $x^{10}$ was the model with the highest $r$ value with a 79\% correlation to the raw data. The model revealed that, similar to my hypothesis, there was a correlation between having a more "extreme" ranking, with the relative maximums completing their rise or decent from the $20 \%$ SpP rate mark within the top and bottom 5 ranked teams. This could have several implications - perhaps poor playing teams are using it at the wrong times due to ineffective statistical analysis, or they are using it to compensate for other aspects of their team. Better playing teams may simply being using it more effectively and with less error - either due to the superiority of their analysis or simply due to having better players. Meanwhile, middling teams seem to opt out and reap neither the reward nor the risk of shifting, as demonstrated by their placement in the middle of the rankings.

My data, of course, has flaws; I used a limited sample in comparison to the vast amount of data available for the MLB, and specifically only sourced from one season, which offers a limited idea of how shifting is continually being used across seasons. Too, the expansion of data points may allow for a more relevant model; while my data had an $r$ value of 0.79 and therefore is strongly correlated, a more comprehensive data set could lead to more powerful models. Topics such as this, which explore the more specific cases of shifting and who uses it, could be even more expansive in looking at how this strategy may be changing the game, something I hope to address in the future.

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## Appendix A

| League |  |  |  |  | vs R |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | PA | Shifts | Shift \％ | PA | Shifts | \％ | wOBA | PA | Shifts | \％ | wOBA |
| 2019 | 184392 | 47178 | 25.6 | 108892 | 15548 | 14.3 | ． 350 | 75500 | 31630 | 41.9 | ． 330 |


|  |  |  |  |  |  | vs RHH |  |  |  | vs LHH |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rk． | Year | Team | PA | Total Shifts | \％ | PA | Shifts | \％ | wOBA | PA | Shifts | \％ | wOBA |
| 1 | 2019 | If Dodgers | 5884 | 2975 | 50.6 | 3538 | 1493 | 42.2 | ． 302 | 2346 | 1482 | 63.2 | ． 293 |
| 2 | 2019 | （1）Astros | 5922 | 2934 | 49.5 | 3243 | 862 | 26.6 | ． 308 | 2679 | 2072 | 77.3 | ． 277 |
| 3 | 2019 | \％Orioles | 6381 | 2732 | 42.8 | 3754 | 1095 | 29.2 | ． 381 | 2627 | 1637 | 62.3 | ． 339 |
| 4 | 2019 | $\mathrm{T}_{\mathrm{B}}$ Rays | 6059 | 2255 | 37.2 | 3777 | 1248 | 33.0 | ． 323 | 2282 | 1007 | 44.1 | ． 282 |
| 5 | 2019 | M Marlins | 6146 | 2238 | 36.4 | 3472 | 760 | 21.9 | ． 362 | 2674 | 1478 | 55.3 | ． 352 |
| 6 | 2019 | $\mathbb{N}$ Yankees | 6027 | 2168 | 36.0 | 3737 | 766 | 20.5 | ． 378 | 2290 | 1402 | 61.2 | ． 310 |
| 7 | 2019 | 历Twins | 6236 | 2216 | 35.5 | 3686 | 1287 | 34.9 | ． 323 | 2550 | 929 | 36.4 | ． 326 |
| 8 | 2019 | （3）Brewers | 6223 | 2124 | 34.1 | 3621 | 692 | 19.1 | ． 379 | 2602 | 1432 | 55.0 | ． 338 |
| 9 | 2019 | A D－backs | 6164 | 2002 | 32.5 | 3477 | 698 | 20.1 | ． 350 | 2687 | 1304 | 48.5 | ． 320 |
| 10 | 2019 | P Pirates | 6325 | 1910 | 30.2 | 3692 | 718 | 19.4 | ． 405 | 2633 | 1192 | 45.3 | ． 377 |
| 11 | 2019 | 运 Tigers | 6237 | 1830 | 29.3 | 3967 | 539 | 13.6 | ． 384 | 2270 | 1291 | 56.9 | ． 354 |
| 12 | 2019 | ＊Blue Jays | 6287 | 1789 | 28.5 | 3471 | 422 | 12.2 | ． 364 | 2816 | 1367 | 48.5 | ． 333 |
| 13 | 2019 | C Reds | 5944 | 1606 | 27.0 | 3156 | 229 | 7.3 | ． 272 | 2788 | 1377 | 49.4 | ． 317 |
| 14 | 2019 | 军 Giants | 6230 | 1581 | 25.4 | 3849 | 636 | 16.5 | ． 353 | 2381 | 945 | 39.7 | ． 316 |
| 15 | 2019 | 掝 White Sox | 6096 | 1357 | 22.3 | 3558 | 291 | 8.2 | ． 391 | 2538 | 1066 | 42.0 | ． 323 |
| 16 | 2019 | T Rangers | 6343 | 1359 | 21.4 | 3802 | 429 | 11.3 | ． 382 | 2541 | 930 | 36.6 | ． 324 |
| 17 | 2019 | A＇s Athletics | 6008 | 1156 | 19.2 | 3202 | 133 | 4.2 | ． 315 | 2806 | 1023 | 36.5 | ． 296 |
| 18 | 2019 | ff Mariners | 6153 | 1175 | 19.1 | 4010 | 226 | 5.6 | ． 353 | 2143 | 949 | 44.3 | ． 339 |
| 19 | 2019 | $\mathbb{G}^{\text {R }}$ Rockies | 6386 | 1197 | 18.7 | 3568 | 290 | 8.1 | ． 356 | 2818 | 907 | 32.2 | ． 369 |
| 20 | 2019 | 3 Red Sox | 6198 | 1141 | 18.4 | 3953 | 38 | 1.0 | ． 478 | 2245 | 1103 | 49.1 | ． 338 |
| 21 | 2019 | FC Royals | 6163 | 1101 | 17.9 | 3463 | 364 | 10.5 | ． 315 | 2700 | 737 | 27.3 | ． 369 |
| 22 | 2019 | P Phillies | 6197 | 1057 | 17.1 | 3700 | 274 | 7.4 | .430 | 2497 | 783 | 31.4 | ． 379 |
| 23 | 2019 | A Angels | 6145 | 1033 | 16.8 | 3721 | 560 | 15.0 | ． 405 | 2424 | 473 | 19.5 | ． 317 |
| 24 | 2019 | 芽 Padres | 6141 | 1023 | 16.7 | 3665 | 319 | 8.7 | ． 292 | 2476 | 704 | 28.4 | ． 343 |
| 25 | 2019 | \＄Cardinals | 5915 | 934 | 15.8 | 3267 | 115 | 3.5 | ． 452 | 2648 | 819 | 30.9 | ． 320 |
| 26 | 2019 | A Braves | 6209 | 924 | 14.9 | 3936 | 339 | 8.6 | ． 368 | 2273 | 585 | 25.7 | ． 354 |
| 27 | 2019 | （0）Nationals | 6093 | 872 | 14.3 | 3570 | 116 | 3.2 | ． 375 | 2523 | 756 | 30.0 | ． 320 |
| 28 | 2019 | Hets | 6153 | 870 | 14.1 | 3770 | 221 | 5.9 | ． 309 | 2383 | 649 | 27.2 | ． 345 |
| 29 | 2019 | C．Indians | 5989 | 840 | 14.0 | 3345 | 96 | 2.9 | ． 276 | 2644 | 744 | 28.1 | ． 311 |
| 30 | 2019 | （C）Cubs | 6138 | 779 | 12.7 | 3922 | 292 | 7.4 | ． 370 | 2216 | 487 | 22.0 | ． 322 |

## Key：

Red：Above Average Shift per Play Percentage

Blue：Below Average Shift Per Play Percentage

